
Calcolo di un limite con il teorema dei Carabinieri

File scaricato da <http://www.extrabyte.info>

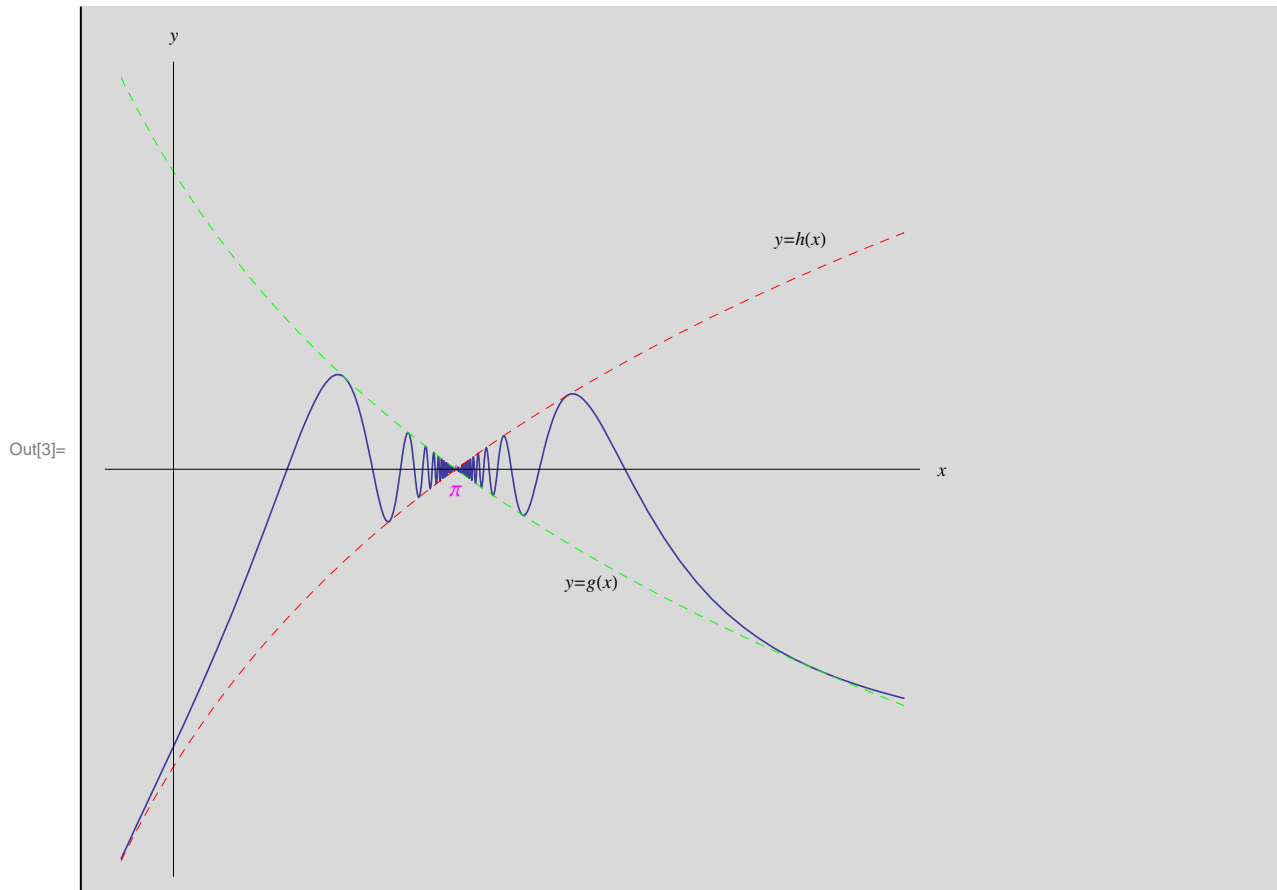
```
In[1]:= f[x_] := Sin[ $\frac{1}{\text{Sin}[x]}$ ] Sin[x]; h[x_] := Log[x]; g[x_] := -Log[x]
```

```
In[2]:= Limit[  
  f[x],  
  x  $\rightarrow$   $\pi$   
]
```

```
Out[2]= 0
```

In[3]:=

```
plots = Plot[
  {
    Sin[ $\frac{1}{\sin[x]}$ ] Log[Abs[(x -  $\pi$ ) + 1]],
    Log[Abs[(x -  $\pi$ ) + 1]],
    -Log[Abs[(x -  $\pi$ ) + 1]]
  },
  {x, 2.5, 4},
  AxesLabel ->
  {
    "x", "y"
  },
  ImageSize ->
  {
    400, 400
  },
  PlotStyle ->
  {
    Thickness[0.002],
    {
      Dashed, Thickness[0.001], Red
    },
    {
      Dashed, Thickness[0.001], Green
    }
  },
  Ticks ->
  {
    { $\pi$ },
    None
  }
  ,
  TicksStyle -> Directive[
    Hue[5/6],
    11
  ],
  AspectRatio -> 1,
  Epilog ->
  {
    Text["y=h(x)", {3.8, 0.6}],
    Text["y=g(x)", {3.4, -0.3}]
  }
]
```



In[4]:= `Limit` [`Sin` [$\frac{1}{\text{Sin}[x]}$] `Log` [`Abs` [$(x - \pi) + 1$]] , `x` $\rightarrow \pi - 1$]

Out[4]= $-\infty$

In[5]:= `Clear` [`plots`]

In[6]:= `x0 = $\pi - 1$;`

```
In[7]:= plots = Plot[
  {
    Sin[ $\frac{1}{\sin[x]}$ ] Log[Abs[(x -  $\pi$ ) + 1]],
    Log[Abs[(x -  $\pi$ ) + 1]]
  },
  {x, x0 - 2, x0 + 0.5},
  AxesLabel ->
  {
    "x", "y"
  },
  ImageSize ->
  {
    400, 400
  },
  PlotStyle ->
  {
    Thickness[0.003],
    {
      Dashed, Thickness[0.001], Red
    },
    {
      Dashed, Thickness[0.001], Green
    }
  },
  Ticks ->
  {
    { $\pi$ ,  $\pi - 1$ },
    None
  }
  ,
  TicksStyle -> Directive[
    Hue[5 / 6],
    11
  ],
  AspectRatio -> 1,
  Epilog ->
  {
    {Dashed, Line[{{ $\pi - 1$ , 0}, { $\pi - 1$ , -4}}]}
  }
]
```

Out[7]=

